Communication with Extraterrestrial Intelligence[1]

BY LAMBROS D. CALLIMAHOS

Unclassified

We are not alone in the universe. A few years ago, this notion seemed farfetched; today, the existence of extraterrestrial intelligence is taken for granted by most scientists. Sir Bernard Lovell, one of the world's leading radio astronomers, has calculated that, even allowing for a margin of error of 5000%, there must be in our own galaxy about 100 million stars which have planets of the right chemistry, dimensions, and temperature to support organic evolution. If we consider that our own galaxy, the Milky Way, is but one of at least a billion other galaxies similar to ours in the observable universe, the number of stars that could support some form of life is, to reach for a word, astronomical. As to advanced (by miserable earth standards) forms of life, Dr. Frank D. Drake of the National Radio Astronomy Observatory at Green Bank, West Virginia, has stated that, putting all our knowledge together, the number of civilizations which could have arisen by now is about one billion. The next question is, "Where *is* everybody?"

The nearest neighbor to our solar system is Alpha Centauri, only 4.3 light years away; but, according to Dr. Su-Shu Huang of the National Aeronautics and Space Administration, its planetary system is probably too young for the emergence of life. Two other heavenly friends, Epsilon Eridani and Tau Ceti, about 11 light years away, are stronger contenders for harboring life. Nevertheless, if superior civilizations are abundant, the nearest would probably be at least 100 light years away; therefore, it would take 200 years for a reply to be forthcoming, a small matter of seven generations. This should, however, make little difference to us, in view of the enormous potential gain from our contact with a superior civilization. Unless we're terribly conceited (a very unscientific demeanor), we must assume that the "others" are far more advanced than we are. Even a 50-year gap would be tremendous; a 500-year gap staggers the imagination, and as _

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[1] The substance of this article was presented at a panel discussion of the same title during the 1965 IEEE Conference on Military Electronics held in Washington, D. C., on 23 September 1965. Besides the author as cryptologist, the other members of the panel were Dr. Paul Garvin, linguist; Dr. John C. Lilly, delphinologist; Dr. William O. Davis, physicist; and Fr. Francis J. Heyden, S. J., astronomer. The moderator was Dr. Harold Wooster, Director of Information Services of the Air Force Office of Scientific Research.

for a 5000-year gap . . . (By the way, if they are as much as 50 years behind us, forget it!) It is quite possible that "others" have satellite probes in space, retransmitting to "them" anything that sounds non-random to the probe. But they have probably called us several thousand years ago, and are waiting for an answer; or worse yet, they have given up; or, more probably, they have reached such impressive technological advances that they have destroyed themselves.[2]

Epsilon Eridani and Tau Ceti were the targets on which Dr. Drake focussed his attention in the spring of 1960 in Project Ozma, an attempt to detect possible intelligent signals from outer space. The frequency selected for listening was 1420.405752 megacycles per second, or a wave length of 21 cm. This particular frequency, postulated independently by two professors on the faculty of Cornell University, Giuseppe Cocconi and Philip Morrison, happens to be the radiation frequency of atomic or free hydrogen which permeates space in great clouds; moreover, this frequency is within the range of radio frequencies able to pass through the earth's atmosphere. Presumably, the significance of this frequency would be known to other intelligent beings in the universe who understand radio theory. We're still talking about radio waves as the communication medium; other possible media might be masers, lasers, or the as-yet undiscovered and unnamed "rasers." A technology superior to ours might even have learned how to modulate a beam of neutrinos (weightless, uncharged particles that physicists on earth find it difficult even to detect); if so, "they" may have to wait a century or two before we learn how to build a neutrino receiver.

If another civilization were trying to establish communication with us, it would first embark on attention-getting signals of such a nature that we could distinguish them from random cosmic noise; once we receive a recognizable signal, we have a good chance of understanding the message. For example, they could start with trains of signals corresponding to the natural numbers 1, 2, 3, . . . , followed perhaps by prime numbers. They might continue with equal-length extended signals consisting of start and stop impulses, with occasional pulses in

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[2] In this connection, Professor Iosif Shklovsky, Russia's greatest radio astronomer, has the following to say in the September 1965 issue of *Soviet Life*:

"Profound crises lie in wait for a developing civilization and one of them may well prove fatal. We are already familiar with several such critical [situations]:

(a) Self-destruction as a result of a thermonuclear catastrophe or some other discovery which may have unpredictable and uncontrollable consequences.

(b) Genetic danger.

(c) Overproduction of information.

(d) Restricted capacity of the individual's brain which can lead to excessive specialization, with consequent dangers of degeneration.

(e) A crisis precipitated by the creation of artificial intelligent beings."

between; when these signals are a would show a circle, the Pythagor design. These attention-getting s "language lessons," interspersed wi help bring us up to the level of our s

It may be assumed that the s possessed by all higher forms of li could thus be greatly simplified i representation such as that of a te held at Green Bank in 1961 to discu with other planets, one of the par up a hypothetical message on ti consisting of 1271 binary digits or 1271 has but two prime factors, 3: to write out the message in raster in 31 lines of 41 bits each; the latte ness in the patterns disclosed, in dimensions. In Fig. 2 is the writ binary 1's have been replaced by a Now for its interpretation.

There are dots at the four cor points, marking the outlines of th representation of the sun; directl representing 8 planets, identified I their left, preceded by a binary r legged beings illustrated are obvic hand of the male figure points to parently reside. At the top of th tions of hydrogen, carbon, and chemical structure of life on their third planet there emerges a wavy water; the representation of a fish and therefore have space travel. to a six (preceded by the usual t there are six fingers on each har their number system is probably female figure may be seen a bracke binary form (preceded by a binar are 11 units high. A reasonable cm., the wave length of the trans. tall, which should be all right for a

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between; when these signals are aligned flush over one another, they
would show a circle, the Pythagorean Theorem, or similar geometric
design. These attention-getting signals would be followed by early
"language lessons," interspersed with items of technical information to
help bring us up to the level of our superiors, "them."

It may be assumed that the sense of sight, or an equivalent, is
possessed by all higher forms of life; the problems of communication
could thus be greatly simplified through the medium of a "raster"
representation such as that of a television screen. After a conference
held at Green Bank in 1961 to discuss the possibility of communication
with other planets, one of the participants, Bernard M. Oliver, made
up a hypothetical message on the raster principle. The message,
consisting of 1271 binary digits or "bits," is shown in Fig. 1. Since
1271 has but two prime factors, 31 and 41, we would naturally be led
to write out the message in raster form, in 41 lines of 31 bits each, or
in 31 lines of 41 bits each; the latter case reveals a greater nonrandom-
ness in the patterns disclosed, indicating that these are the correct
dimensions. In Fig. 2 is the write-out of the message, in which the
binary 1's have been replaced by a dot and the 0's left as blank spaces.
Now for its interpretation.

There are dots at the four corners of the pictogram as reference
points, marking the outlines of the rectangle. At the upper left is a
representation of the sun; directly underneath in a column are dots
representing 8 planets, identified by the appropriate binary coding to
their left, preceded by a binary point as a marker. The erect, two-
legged beings illustrated are obviously bisexual and mammalian; one
hand of the male figure points to the fourth planet where they ap-
parently reside. At the top of the pictogram may be seen representa-
tions of hydrogen, carbon, and oxygen atoms, indicating that the
chemical structure of life on their planet is similar to ours. From the
third planet there emerges a wavy line, showing that it is covered with
water; the representation of a fish shows that they must have visited us
and therefore have space travel. One hand of the female figure points
to a six (preceded by the usual binary point), perhaps implying that
there are six fingers on each hand; we could therefore assume that
their number system is probably to the base 12. At the right of the
female figure may be seen a bracket, in the middle of which is eleven in
binary form (preceded by a binary point): this implies that the beings
are 11 units high. A reasonable interpretation is that the unit is 21
cm., the wave length of the transmission, making them about 7½ feet
tall, which should be all right for average Martians.

In 1952 the British mathematician Lancelot Hogben delivered an
address before the British Interplanetary Society entitled "Astraglossa,
or First Steps in Celestial Syntax." Hogben pointed out that *number*

L. D. C.

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10000000009000000000000000000000000000000000000
100001110000.00.00000100000100000010000100
0000010001000000000000000000000000000000000
0000010000100.0010000001000000100000010000
00000010010000001000000100000001000100
010000000111000000000000000100000000000001
00000000000000000000000000000000000000000
00000000000000000000010000010000000100
0001000011000100000000000110000000000000
00000000000000000011000011000011000000110
110110110100110000110101101011010010 0100
10010010010101001001000011000011000011 00
0011000-011-0000-0-000100000000000011111 0100
0000000000000000000000000000010000000100
0000000010110111001000000000000001111101
00000000000000000000000000100000000000000
0000010000100111000000000000010100000000
00000010100001100101011100101000000000
0000001010010001000000000100100000000
00000001001000010000000000011111000000
00000001110000001110101000001010100000
0000000101010000010000000000010001010
00000001010010000000000000001000100
10010001001101100111011011010000100010
0010101010000100000000000000000010001
0001001001001001000000100000000000111
0000011110000011100000000111101000000101
010000010100000100010000000100000000100
00010001110000100000100000100000000010
0000100010010010010000010000011000110000 1
000001000100010001000001000001100000001
100000110110001101100000110011 1
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Fig. 1.

Fig. 2.

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intelligent beings; therefore, mat:
steps in extraterrestrial communi
could transmit pulses representin
"radioglyphs" representing "+"
later carried out the basic idea :
shapes to represent elementary
different approach was develope
Mathematics at the University
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As an illustration of how much
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let us consider a message I have d
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16 units, respectively. Betwee
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The Rosetta Stone is a piece of blac.
of the Nile, bearing a bilingual inscription
and Greek) with which Jean François Ch
Egyptian hieroglyphs.

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0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 1 0 0
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
0 0 1 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0
0 0 0 1 0 0 0 0 0 0 0 1 0 0 0 1 0 0
0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 1
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
0 0 0 1 0 0 0 0 1 0 0 0 0 0 1 0 0
0 0 0 1 1 0 0 0 0 0 0 0 0 0 0 0 0
1 0 0 0 1 1 0 0 0 0 1 1 0 0 0 0 1 1 0
0 0 1 0 1 1 0 1 0 1 1 0 0 1 0 0 1 0 0
0 0 0 1 1 0 0 0 1 1 0 0 0 0 1 1 0 0
0 0 0 0 0 0 0 0 0 1 1 1 1 0 1 0 0
0 0 0 0 0 0 0 0 0 1 0 0 0 0 1 0 0
0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 1
0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0
0 1 0 1 1 1 0 0 1 0 1 0 0 0 0 0 0 0
0 0 0 0 0 0 1 0 0 1 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 1 1 1 1 1 0 0 0 0
1 0 1 0 1 0 0 0 0 0 1 0 1 0 1 0 0 0
0 0 0 0 0 0 0 0 0 1 0 0 1 0 1 0
0 0 0 0 0 0 0 0 0 0 1 0 0 0 1 0 0
0 1 1 0 1 1 0 1 0 0 0 0 0 1 0 0 0 1 0
0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 1
0 0 0 1 0 0 0 0 0 0 0 0 0 1 1 1
0 0 0 0 1 1 1 1 0 1 0 0 0 0 1 0 1
0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 1 0
1 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 1 0
0 1 0 0 0 0 1 1 0 0 1 1 0 0 0 0 1
0 0 1 0 0 0 0 1 1 0 0 0 0 0 0 0 1
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is the most universal concept for establishing communication between intelligent beings; therefore, mathematics forms the basis for the first steps in extraterrestrial communication. He then illustrated how he could transmit pulses representing integers, and distinctive signals or "radioglyphs" representing "+", "−", "=", and so on. Morrison later carried out the basic idea a little further, using different pulse shapes to represent elementary mathematical symbols. An entirely different approach was developed by Hans Freudenthal, Professor of Mathematics at the University of Utrecht, who in 1960 published a book entitled "Lincos: Design of a Language for Cosmic Intercourse." "Lincos," an acronym of "lingua cosmica," tries to establish a communication of ideas through symbolic logic, but the general consensus of those who have taken the trouble to study his book is that his plan is too difficult. After all, the object of the exercise is getting ideas across to another party, whose thinking processes may be entirely different from our own. In other words, what we need to develop is an "inverse cryptography," or communication symbolism specially designed, not to hide meaning, but to be as *easy* as possible to comprehend. Cleverness on the part of the *sender* is then the important factor, not reliance on ingenuity of the recipient. The inverse cryptographer—somehow, this term doesn't sound quite right—must make his meaning clear to the recipient, even if the latter does not possess a cosmic equivalent of the Rosetta Stone.[3]

As an illustration of how much information could be conveyed with a minimum of material, and as an example of facile inverse cryptography, let us consider a message I have devised to be typical of what we might expect of an initial communication from outer space. In Fig. 3 is shown a series of transmissions which could have come from another inhabited planet, many light years away. The 32 arbitrary symbols are representations for the 32 different signals (combinations of beeps, or distinctive pulse shapes) heard on a frequency of 1420.4 megacycles. The punctuation marks are not part of the message, but here represent different time lapses: adjacent symbols are sent with a short pause (1 unit) between them; a space between symbols means a longer pause (2 units); commas, semicolons, and periods indicate pauses of 4, 8, and 16 units, respectively. Between transmissions (numbered here for reference purposes) there is a time lapse of 32 units.

The first transmission, (1), is obviously an enumeration of the 32 different symbols which will be used in the communications; in transmission (2) is the clear implication that A represents the integer 1, B

[3] The Rosetta Stone is a piece of black basalt found in 1799 near the Rosetta mouth of the Nile, bearing a bilingual inscription (in Egyptian hieroglyphics, Egyptian demotic, and Greek) with which Jean François Champollion was able to solve the mystery of the Egyptian hieroglyphs.

(1) A. B. C. D. E. F. G. H. I. J. K. L. M. N. O. P. Q. R. S. T. U. V. W. X. Y. Z.
     •. &. $. ¢. ƒ. @.   A. B. C. D. E. F. G. H. I. J. K. L. M. N. O. P. Q. R.
     S. T. U. V. W. X. Y. Z. •. &. $. ¢. ƒ. @.

(2) A A. B: A A A. C: A A A A. D: A A A A A. E: A A A A A A. F: A A A A A A A. G:
     A A A A A A A A. H: A Ł A A A A A A A. I: A A A A A A A A A A. J.

(3) A K A L B: A K A K A L C: A K A K A K A L D. A K A L B: B K A L C: C K A L D.
     B K C L E: E L B K C: F K D L J: J L D K F. E L K E: K E L E.

(4) C K A L B: D K A L C: G K E L B: E K C L M B.

(5) D K N L D: C K N L G: F K F L N: E M E L N.

(6) J L AN: J K A L AA: J K B L AB: AA K A L AB. J K J L BN: J K J K J L CN:
     IN K C L IC.

(7) B O C L F: D O B L AN: E O B L AN: D O AN L DN.

(8) F P C L B: H P B L D: J P B L E: J P E L B.

(9) A P J L Q J: A P ANN L Q ANN: Q J. P J L Q ANN.

(10) Q J L R A: Q J O B L R B: A R E M A L R E L E O Q J. Q ANN L R NA:
     Q ANN O B L R NB.

(11) H L H: G S C. C S G.. D K A L C K B: D K C S E K A: E K A S D K C.

(12) D T A: D T B: D T C: D L D: D U E: D U F: D U G. J T I: J U AA.

(13) FIRII V GN: ANN K C V ANN: AN P C V CRC.

(14) W E K A X L E K A: B W E K A X L W B O E X K W B O A X L B O F.

(15) C Y B L I: E Y B L BE: B Y E L CB: W D K A X Y B L EE.

(16) BE Z B L E: FD Z B L H: BG Z C L C: ABE Z C L E. W AI K F X Z B L E.
     EE Z B_L M E: M ABE Z C L M E. BE Z B L KM E.

(17) D • L D O C O B O A L BD: E • L E O D O C O B O A L ABN: H • L DNCEN.

(18) Ł P D Ł A M Q C K Q E M Q G K Q I M. & V CRADAEI.

(19) S L A K Q W A • X K Q W B • X K Q W C • X K Q W D • I X. S V BRCANEH.

(20) ¢ E K A ƒ L W E K A X: B ¢ E K A ƒ L B W E K A X:
     B ¢ E K W D K C X ƒ L B W E K C X. ¢ B ƒ ¢ D ƒ L W B X W D X L B O D.

(21) S Y ¢ & O W M A X Z B ƒ K A L M.

(22) B K C L ¢ @NAA ƒ: B K C L E. C O D L ¢ @NAA ƒ: C O D L AB.
     D Y B L ¢ @NAA ƒ: D Y B L AF.

(23) B K C L E: ¢ @NNB ƒ. B K D L E: ¢ @NNC ƒ. E Y B L BE: ¢ @NNB ƒ. F Y B L C E:
     ¢ @NNC ƒ. I T E: ¢ @NNB ƒ. H U C: ¢ @NNC ƒ. & V BRCANEH: ¢ @NNC ƒ.

(24) B L ¢ @NNO ƒ. C L ¢ @NNO ƒ. E, G, AA, AC, AG, ¢ @NNO ƒ. ANA ¢ @NNO ƒ.

(25) ¢ @NNG ƒ L B O ¢ @NN ƒ: ¢ @NNF ƒ L ¢ @NN ƒ Y B. ¢ @A ƒ L ¢ @NNC ƒ.
     ¢ @NNE ƒ L B ¢ @NNC ƒ: ¢ @NNF ƒ L ¢ @NNG ƒ Y B.

(26) ¢ @NNH ƒ L D O Q C O ¢ @NNG ƒ Y C.

(27) Q B K Q D K Q H K Q AF K Q CB V A:
     Q B K Q D K Q H K Q AF K Q CB K ¢ @NNI ƒ L A.

(28) C K ¢ @A ƒ L C: ¢ @A ƒ L D. I K ¢ @A ƒ L AB: ¢ @A ƒ L C.
     FD Z ¢ @A ƒ L H: ¢ @A ƒ L B.
     ¢ @A ƒ L A, R CC, M R CC, J P C, &, K, M, ¢ @NNI ƒ.
     ¢ @B ƒ L A, R CC, M R CC, J P C, &, K, M, ¢ @NNI ƒ.
     ¢ @C ƒ L A, R CC, M R CC, J P C, &, K, M, ¢ @NNI ƒ.

(29) ¢ @NNE ƒ L B & ¢ @B ƒ: ¢ @NNF ƒ L & ¢ @B ƒ Y B.
     ¢ @NAN ƒ L B ¢ @C ƒ K B ¢ @D ƒ: ¢ @NAA ƒ L ¢ @C ƒ O ¢ @D ƒ.

(30) ¢ @NNE ƒ L ¢ @NAB ƒ: ¢ @NAO ƒ: ¢ @NNF ƒ L ¢ @NAD ƒ, ¢ @NAC ƒ.
     ¢ @NAN ƒ L ¢ @NAB ƒ, ¢ @NAE ƒ: ¢ @NAA ƒ L ¢ @NAD ƒ, ¢ @NAE ƒ.

Fig. 3.

the integer 2, . . . , J the integer
there are introduced symbols for
in teaching us their mathemat
addition, subtraction, multiplic:
and the concept of zero; inequa
roots; and definitions of π and
new to the 31 symbols recovered
most beautiful concepts in pure
if they can teach us such a com-
be staggered by what they will
transmission.   Beginning with
cluster concepts are introduce
transmission (30), we now are u:
pure Venerean.   Furthermore,
the code they are using on us
thousands upon thousands of
this is easily appreciated by an
the meaning of all 30 transmissi

Even right after this first mes-
with that planet, we shall have
Fermat's Last Theorem, Golc
unsolved problems in mathem:
not be difficult for "them" to c
nological superiority (first of a
able to call us!).   If "they" b
structure constant," they are a:
five for sure, suspect the sixth,
ratio, among others, of the spec
electron; it may take a century
And after we resolve our pres
appropriate to make discreet
harmony and peace with our fe:
otherwise ingested by the su
fortune to contact us.   But as
(and generations of his descend:

‘ The solution may be found on p. :
⁵ With what he has learned from
reader formulate these two questions o
compact form; the solutions appear on
classic unsolved problems in mathemati
values of x, y, and z can be found
is an integer greater than 2; Goldbach's
other mathematicians failed to make t:
number greater than 2 can be expressed

N. O. P. Q. R. S. T. U. V. W. X. Y. Z.
F. G. H. I. J. K. L. M. N. O. P. Q. R.
S.

. E: A A A A A A. F: A A A A A A A. G:
I: A A A A A A A A A; J. – – –

. L D. FKIL B; B K A L C: C K A L D. ~
K F. E L X E: K E L E.   – – – –

L M B. ..   – –

L N. =   – . –

L AB. J K J L BN: J K J L CN:

N L DN.

L S.

L Q ANN.

E L E O Q J. Q ANN L R NA:

K C S E K A; E K A S D K C.

F: D U G. J T I: J U AA.

C.

S X K W B O A X L B O F.

: A X Y S L SE.

Z C L E. W AI K F X Z B L E.
. KN E.

C C.B O A L ABN: H · L DNCBN.

V CRADAZI.

X K Q W D · X K. S V BRCAHBN.

: E K A X:
c D # L W B X W D X L S O D.

@NNA #: C O D L AB.

: #. E Y B L BE: c @NNB #. F Y B L C E:
@NNC #. L V BRCAHBN: c @NNC #.

AC. AC. c @NND #. ANA c @NND #.

. c @A # Y S. c @A # L c @NNG #.

. c @NNG # Y B.

L A.

L AB: c @A # L C.

% c @ NNT #. – – – –
L. c @ NNI #.
L. c @ NNI #.

@3 # Y B.
M # L c @C # O c @D #.

L c @NAD #, c @ NAC #.
L c @NAD #, c @ NAE #.

the integer 2, . . . , J the integer 10. In the first twenty transmissions there are introduced symbols for the introductory expository treatment in teaching us their mathematics. Among the items treated are: addition, subtraction, multiplication, and division; decimal notation and the concept of zero; inequalities and approximation; powers and roots; and definitions of π and e. Transmission (21) adds nothing new to the 31 symbols recovered thus far, but it does quote one of the most beautiful concepts in pure mathematics: they are telling us that, if they can teach us such a complex notion at this early stage, we will be staggered by what they will teach us by the 200th or the 2000th transmission. Beginning with transmission (22), words and word-cluster concepts are introduced, so that by the time we come to transmission (30), we now are understanding, in a manner of speaking, pure Venerean. Furthermore, we can now see how we could recover the code they are using on us, and which will obviously consist of thousands upon thousands of code groups with different meanings; this is easily appreciated by anyone who takes the trouble to fathom the meaning of all 30 transmissions in the foregoing example.[4]

Even right after this first message, if we are in direct communication with that planet, we shall have questions to put to "them": the proof of Fermat's Last Theorem, Goldbach's conjecture,[5] and many other unsolved problems in mathematics and the natural sciences. It will not be difficult for "them" to demonstrate their intellectual and technological superiority (first of all, don't forget it was *they* who were able to call *us*!). If "they" but know the *seventh* digit of the "fine structure constant," they are ages ahead of us (we know only the first five for sure, suspect the sixth). This number, 137.039 . . . , is the ratio, among others, of the speed of light to the speed of the hydrogen electron; it may take a century to calculate this constant to 9 digits. And after we resolve our pressing scientific questions, it might be appropriate to make discreet inquiries as to how we could live in harmony and peace with our fellow man—that is, if we aren't eaten or otherwise ingested by the superior civilization that had the good fortune to contact us. But as far as the cryptologist is concerned, he (and generations of his descendants who might experience the supreme

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[4] The solution may be found on p. 109; but eschew the premature peek.

[5] With what he has learned from this example of space communication, let the reader formulate these two questions directly for transmission to "them," in a clear and compact form; the solutions appear on pg. 109. For the reader who is a little rusty on classic unsolved problems in mathematics, Fermat's Last Theorem states that no integral values of x, y, and z can be found to satisfy the equation $x^n + y^n = z^n$, if n is an integer greater than 2; Goldbach's "notorious" conjecture ("notorious" only because other mathematicians failed to make the conjecture themselves) states that every even number greater than 2 can be expressed as the sum of two primes.

thrill of their lives when we hear from "them") must keep a level head, not get excited, and be prepared to cope with problems the like of which he has never seen—out of this world, so to speak.

Electroni(

BY JOHN

Top S

INTRODUCTION

Calligraphy, the art of produ
familiar term in the English lan;
letters in its alphabet, English r
manual or mechanical. Slight
tions have little effect on legib
texts are easily obtained due to
All that is necessary is a unique :
it is a typewriter key or a con
English requires only that a sig:
letter. The Morse and Baudot
sult of such transmissions is ea:

Generally speaking, most alp;
graphic problems. However, s(
graphic in nature. Such langu;
sent some idea or thing. Altho
rules of formation, the number
often very large. For exampl
thousand unique ideographs. I:
as a single element. The follow:
lar symbols with very dissimilar r

Character

千 -------

米 ------

オ ------

木 ------

禾 ------

Therefore, for these languages,
tention in order to obtain intelli

Symbols

A	1	I	9	Q	reciprocal	Y	power
B	2	J	10	R	decimal point	Z	root
C	3	K	+	S	$\neq$	"	factorial
D	4	L	=	T	>	&	$\div$
E	5	M	−	U	<	$	e
F	6	N	Ø	V	$\approx$	¢	[
G	7	O	$\times$	W	(	$\neq$	]
H	8	P	÷	X	)	@	code

Code values

001 question	007 radius	013 circle
002 true	008 volume or sphere	014 area
003 false	009 ... (ellipsis)	015 rectangle
004 prime	010 perimeter of rect.	.
005 circum. of circle	011 area of rectangle	.
006 area of circle	012 perimeter	999

Code values 1, 2, 3 . . . 99 = x, y, z . . . (abstractions, unknowns, variables).

Fermat's Last Theorem:

¢@A $\neq$ Y ¢@D $\neq$ K ¢@B $\neq$ Y ¢@D $\neq$ L ¢@C $\neq$ Y ¢@D $\neq$. ¢@D $\neq$ L B;
¢@NNB $\neq$. ¢@D $\neq$ L C, D, E, ¢@ NNI $\neq$; ¢@NNB NNA $\neq$.

Goldbach's Conjecture:

B ¢@A $\neq$. B ¢@A $\neq$ L ¢@B $\neq$; ¢@B $\neq$ T B. ¢@B $\neq$ L ¢@C $\neq$ K ¢@D $\neq$;
¢@C $\neq$ L ¢@NND $\neq$, ¢@D $\neq$ L ¢@NND $\neq$. ¢@NNB NNA $\neq$.

Solution to Mr. Callimahos' Space Communication.